CODING LIMITS FOR SHORT RANGE WIRELESS INFRARED TRANSMISSION

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ABSTRACT

Wireless infrared is an attractive alternative for short-range indoor communications. However, mainly as a result of the physical properties of the detector, one serious problem is the power efficiency of the transmission. Under the assumptions of a fixed average optical power and additive white Gaussian noise, we derive the maximum coding gains attainable with optimized On-Off Keying, where "optimized" refers to the probability of the logical "1" pulses in the transmitted data stream. Uncoded On-Off Keying acts as the reference scheme. We also consider orthogonal pulse-position modulation, having favorable spectral characteristics, with and without additional coding and compare the corresponding coding gains with the limits for binary transmission.

1. INTRODUCTION

IR radiation exhibits a number of characteristics which qualify it as a concrete alternative to radio frequency (RF) for short range indoor transmission. First of all, IR takes advantage of a completely unregulated and unlicensed spectral range with a bandwidth of several THz. Since IR radiation does not propagate through walls, systems operating in separate rooms do not interfere with each other; additionally, the optical medium promises high security against eavesdropping.

However, beside these advantages it is known that IR transmission is associated with some serious problems. One of the most challenging is the limited power efficiency. As shown in [1], if IR is directly compared to RF transmission, IR suffers first of all from a strongly reduced receiver sensitivity. IR loses against RF mainly as a result of the different physical principles of the detectors. While the radiation power is available at the output of an antenna as electrical power, the IR detector converts it to a current. The magnitude of this current is physically limited by the photodiode's sensitivity. Even if only the noise generated by the first input stage of the IR-detector is considered, the receiver sensitivity is much worse than in the RF-case.

However, it is well known that the noise of an IR-detector is mainly determined by the shot noise caused by received background light. Since the first diffuse 1 Mb/s IR-system was proposed by Gfeller [2] in 1979, great efforts have been made to increase power efficiency (as well as the data rate) of non-directional arrangements. Besides classical approaches such as power efficient modulation schemes, non-imaging concentrators or optical filters in the last decade techniques using transmitter and receiver arrays to divide the covered angular range into different sectors have become more and more important [3, 4].

The main purpose of this paper is to discuss the advantages in regard to the power efficiency which can be attained due to channel coding. We consider only coding limits and do not propose practical implementations of coding schemes — with the exception of Pulse-Position Modulation (PPM) which can be considered a coding scheme. The investigations are made under the assumptions of a fixed average optical power and white Gaussian receiver noise, which is assumed independent form the signal. These constraints are not applicable for fiber optics or highly directed optical free space links (for instance for satellite communications). For this reason we focus only on non-directed short range wireless IR indoor-transmission. Additionally, only binary (and necessarily unipolar) transmission is considered, where "binary" refers to the possible variation of the pulse amplitudes, i.e., PPM is also considered. Subcarrier (or multiple subcarrier) modulation will not be taken into account, since a further power efficiency drawback is introduced by the required DC-component [5].

In the next section we introduce an OOK (On-Off Keying) transmission model. Note that OOK is equivalent to unipolar binary transmission. It follows the description of the reference transmission scheme: throughout the paper, uncoded OOK acts as the reference in regard to the coding gains and the code rates. In the two major sections 4 and 5, the maximum coding gains attainable with optimized OOK-transmission and with PPM are derived and discussed.

2. OOK TRANSMISSION MODEL

As a result of the limited temporal coherence of the optical transmitters commonly used and the inherent spatial diversity provided by large area photodiodes, it is straightforward to model the optical channel as a linear time invariant system, taking optical instantaneous powers (and not amplitudes) as its input and output. The photodiode with sensitivity $R$, however, converts the impinging optical power into a current, which is an amplitude. Throughout the paper, distortion-less transmission is assumed, i.e., the photodiode is fully described by $R$, the channel impulse response is $h(t) = \delta(t)$.

In the case of OOK, the transmitted optical signal $p_{tx}(t)$ can be denoted as

$$p_{tx}(t) = \sum_{i} s_i \psi(t - iT),$$  \hspace{1cm} (1)

where $\psi(t - iT)$ is the underlying waveform used to "convert" the $i$-th binary symbol $s_i$, $s_i \in \{0, 1\}$, to the continuous optical channel. Clearly, since $p_{tx}(t)$ must be real valued and positive, the

\[E_b/N_0\] should be noted that the "practical" $E_b/N_0$ ratio commonly used for linear AWGN-channels fails for the quadratic channel considered here, since the required optical power does not linearly increase with the bit rate.
the noise power density is mainly determined by the amount of the
or the validity of the assumption that the noise power spectral den-
sity is typically fully independent from the signal
information under the fixed average power assumption.

Transmission takes place under the constraint of a fixed aver-
age optical power \( P \). If the probability of a transmitted symbol \( S \) (corresponding to a binary \( ‘1’ \)) is denoted as \( p_1 \), \( P \) is given by

\[
P = \lim_{T \to \infty} \frac{1}{T} \int_{-T}^{T} p_1(t) \ dt = \frac{1}{T} \int_{-T}^{T} \psi(t) \ dt.
\]

(3)

Note that \( p_1 = 0.5 \) always maximizes the entropy at the channel
input. However, since we assume intensity modulation and direct
detection, the noise source is located in the
square of the transmitted or received optical power. How-
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The receiver consists of a photodiode with sensitivity \( R \), a
matched filter having the impulse response \( \psi(t) \), and a sampling
process. In the considered binary case, the undisturbed sig-
nal amplitudes \( X \) at the sampling times \( t \) can be either zero or
\( X = R \tilde{S} \), which can be expressed as a function of \( P \) and \( T \) as
follows

\[
\tilde{X} = R \tilde{S} = \sqrt{\frac{T}{P}} \frac{R \cdot P}{\int_{-\infty}^{\infty} \psi(x) \ dx}.
\]

with \( x = t/T \) and \( \tilde{\psi}(x) = \sqrt{T} \psi(x \cdot T) \).

(4)

To show that \( \tilde{X} \) in fact depends on \( \sqrt{T} \), we have introduced a
normalized version \( \tilde{\psi}(x) \) of the waveform \( \psi(t) \) in (4). The dimen-
sionless function \( \tilde{\psi}(x) \) and the corresponding integral \( \int_{-\infty}^{\infty} \tilde{\psi}(x) \ dx \)
are effectively a measure of the waveform shape — independent
from the actual symbol duration \( T \), as illustrated in Fig. 2.

Eqn. (4) shows that the system-theoretic power of \( \tilde{X} \) depends
on the square of the transmitted or received optical power. How-

However, the noise source \( n(t) \) in Fig. 1 is located at the output of the
photodiode, thus it is the photocurrent itself which exhibits an ad-
ditional Gaussian distributed, zero-mean white noise component 1.

It is beyond the scope of this article to discuss the origins of \( n(t) \) or the validity of the assumption that the noise power spectral den-
sity is really white (see e.g. [6, 7]), but it should be noted that
\( n(t) \) is typically fully independent from the signal \( p_1(t) \); instead,
the noise power density is mainly determined by the amount of the

\footnotetext{1}{system-theoretic energy}

\footnotetext{2}{If an incoherent RF-detector is considered instead, which may also
exhibit a quadratic detection characteristic, the noise source is located in
front of the nonlinear device and not at the output. This leads to a totally
different conclusion.}

To derive the coding gain limits in the next section, the required
optical power \( P = P_{ref} \) of uncoded OOK-transmission guaran-
teeing a certain bit error probability \( p_e \) will be used as a reference.

Taking \( \psi(t) \) as a unit energy base function, the Euclidian dis-
tance \( d_{Eucl} \) between the two possible values of \( X \) depicted in the
(one dimensional) signal space is equal to \( \tilde{X} \). Supposing \( p_1 = 0.5 \) as well as uncoded transmission, the bit error probability of OOK
is therefore

\[
p_e = \frac{1}{2} \text{erfc} \left( \frac{1}{2 \sqrt{N_0}} \cdot \frac{d_{Eucl}}{\sqrt{N_0}} \right) = \frac{1}{2} \text{erfc} \left( \frac{1}{2 \sqrt{N_0}} \cdot \frac{\tilde{X}}{\sqrt{N_0}} \right).
\]

(6)

From (6) we can at first deduce an OOK reference value

\[
\tilde{X}_{\text{ref}} = 2 \sqrt{N_0} \cdot \text{erfc}^{-1}(2p_e).
\]

(7)
which depends on the required value of $p_e$. Using (4) and setting $T = T_b$, this value corresponds to

$$P_{ref} = \frac{\int_{-\infty}^{\infty} \psi(x) \, dx}{R} \cdot \sqrt{\frac{N_0}{T_b}} \cdot \text{erfc}^{-1}(2p_e) ,$$  \hspace{1cm} (8)

where $1/T_b$ is the bit rate being equal to the symbol rate $1/T$ if no coding is applied.

Although the primary focus of (8) is to act as a reference, this equation gives useful insights in different parameter dependencies for both coded and uncoded transmission:

1. If the bit-rate $1/T_b$ is increased by one decade, and all the other parameters remain fixed, the required power increases only by a factor $\sqrt{10}$ corresponding to 5 dB and not by 10 dB as in the case of a linear channel.

2. Assuming the transmission of a large number $N$ of bits (a "packet"), the required optical energy $NT_bP_{ref}$ decreases by a factor $\sqrt{10}$ if the data rate is increased by a factor 10.

3. Even if a distortion-less channel is considered, the required average power depends on the pulse shape — quite in contrast to linear channels. Furthermore, replacing $\psi(t)$ by an $a$-times "shorter" unit energy version $\psi_0(t) = \sqrt{a} \cdot \psi(at)$ results in $\int_{-\infty}^{\infty} \psi_0(x) \, dx = \sqrt{a} \int_{-\infty}^{\infty} \psi_0(x) \, dx$, which is equivalently a factor $\sqrt{a}$ power advantage compared to the original situation — supposing that the first Nyquist-criteria is still satisfied. In other words: every factor 2 reduction of the pulse width reduces the required power by 1.5 dB, Fig. 2 shows an example.

Throughout the paper we define the code rate $R_c$ as the ratio between the actual binary symbol interval $T$ and $T_b$:

$$R_c = \frac{T}{T_b} .$$  \hspace{1cm} (9)

The coding gain $G$

$$G = \frac{P_{ref}}{P}$$  \hspace{1cm} (10)

is defined as the ratio between the OOK-reference power $P_{ref}$ and the actual required average optical power $P$ to assure a certain bit error probability $p_e$. In (10), the parameters $N_0$, $T_b$, $R$ as well as the pulse shape $\psi(x)$ are supposed to be fixed. Using (10), $X$ can also written as a function of $G$ and $R_c$:

$$\bar{X} = \bar{X}_{ref} \cdot \left( \frac{\sqrt{R_c}}{G} \right) \cdot \frac{0.5}{p_1} .$$  \hspace{1cm} (11)

4. CODED OOK TRANSMISSION

4.1. Mutual information for OOK

Taking $X$ and $Y$ as the random variables at the channel’s input and (soft) output, respectively, the mutual information $H(X; Y)$ is given as

$$H(X; Y) = H(Y) - H(Y|X) ,$$  \hspace{1cm} (12)

where the differential entropy of $Y$ is

$$H(Y) = \int_{-\infty}^{\infty} f_Y(y) \log_2 f_Y(y) \, dy,$$

and

$$H(Y|X) = 0.5 \cdot \log_2(\pi e N_0)$$

is the irrelevance due to the Gaussian noise $N$ described in (5). In the binary transmission case considered here, the probability density function $f_Y(y)$ of the random variable $Y$, required to calculate $H(Y)$, is given as

$$f_Y(y) = \frac{1 - p_1}{\sqrt{\pi N_0}} \exp \left( - \frac{y^2}{N_0} \right) + \frac{p_1}{\sqrt{\pi N_0}} \exp \left( - \frac{(y - \bar{X})^2}{N_0} \right) ,$$

where $\bar{X}$ is already defined in (11).

Fig. 3 shows $H(X; Y)$ for different quotients $(G/\sqrt{R_c})$ as a function of $p_1$. Obviously, if $(G/\sqrt{R_c}) > 1$, the maximum mutual information is not obtained for $p_1 = 0.5$.

4.2. Capacity and coding gain

To calculate the maximum gains attainable with OOK-transmission, $H(X; Y)$ has to be maximized over $p_1$. If the (very small) influence of the "allowed" bit error probability $p_e$ on the required capacity is neglected, the capacity $C$ per binary symbol

$$C = \max_{p_1} H(X; Y)$$  \hspace{1cm} (13)

must be as high as the code rate $R_c$, i.e., $C \geq R_c$. To study the achievable coding gains, we have chosen $p_e = 1 \cdot 10^{-6}$ for the uncoded OOK-reference.

The solid line in Fig. 4 shows the coding gain $G$ in dB as a function of the code rate $R_c$. The pulse density $p_1$ was optimized numerically. Fig. 5 shows the corresponding pulse densities $p_1$ (solid line). As depicted in Fig. 3 already, a code rate $R_c = 0.5$ promises a coding gain of 9.2 dB; this gain requires a pulse density of about $p_1 = 1/7$. If the code rate is further decreased to $R_c = 0.1$, on one hand a gain of as much as 15 dB is attainable, but on the other hand this gain is traded with a very low pulse density, which is close to $p_1 = 1/57$. Low pulse densities may cause several problems: obviously, the optical peak power $\bar{P} = P/p_1$ increases by a factor

$$\frac{\bar{P}}{P_{ref}} = \frac{1}{2G \cdot p_1}$$
Coding gain grows unbounded with since in section 3. it was already derived that a reduction of the varied over 4 decades in Fig. 4. In contrast to linear channels, the pulse width by a factor $\frac{a}{b}$ achieved with attaching a number of.

4.3. Asymptotic behavior

To allow a discussion on the asymptotic behavior, the code rate is varied over 4 decades in Fig. 4. In contrast to linear channels, the coding gain grows unbounded with $1/R_c$. This is not surprising, since in section 3, it was already derived that a reduction of the pulse width by a factor $a$ corresponds to a power advantage of $\sqrt{a}$.

This "shaping gain" is also available in the digital domain. If, for example, the code rate $R_c$ is reduced by a factor $a$ simply by attaching a number of $(a-1)$ zero-symbols to every original symbol $s_i$, which leads automatically to a factor $a$ reduction of $p_1$, the same Euclidian distance $d_{\text{Eucl}}$ between the symbols as before is achieved with $\sqrt{a}$ less optical power, see (11). Hence, the situation at the receiver remains completely unchanged if the zero-symbols attached at the transmitter are discarded at the receiver.

Consequently, to appraise the effectiveness of the coding, the gain $G$ attainable should be weighed with the "trivial" shaping gain, which is $\sqrt{1/R_c}$, to extract the effective gain contributed by the distance-properties of the actual code. This is shown additionally in Fig. 3. It can be seen, that the gain $G$ for $R_c = 0.1$ lies 10 dB over the nominal shaping gain of 5 dB. However, if the code rate is further decreased by 3 decades, the additional gain compared to the 15 dB shaping gain is only 2.5 dB — the actual code provides only a very small additional gain. This may lead to the conclusion that the slope of $G$ over $R_c$ asymptotically reaches a value of 5 dB per decade. Actually, as shown below this is not true at all, since $G \cdot \sqrt{R_c}$ grows unbounded — even though very slowly.

It is a fact that the average required electrical energy per bit $E_b^{(el)}$ of the photo diode current $i_{\text{el}}(t)$ (see Fig. 1) asymptotically reaches a certain fixed value if $R_c$ is decreased steadily. For this case, we denote the fixed ratio between $E_b^{(el)}$ and $N_0$ as $\eta^{(el)}_\infty$:

$$\eta^{(el)}_\infty = \frac{E_b^{(el)}}{N_0} \quad \text{for} \quad R_c \to 0 . \quad (14)$$

The electrical energy at the sampling device can also be expressed using the optical quantities:

$$E_b^{(el)} = \frac{\bar{X}^2}{R_c} \cdot p_1 . \quad (15)$$

Using (7) and (11) it follows for $R_c \to 0$ that

$$\eta^{(el)}_\infty = \frac{\bar{X}^2}{N_0} \cdot \frac{0.5^2}{p_1 \cdot G^2} = \frac{1}{p_1} \left( \frac{\text{erfc}^{-1}(2p_1)}{G} \right)^2 , \quad (16)$$

resulting in a gain

$$G = \frac{1}{\sqrt{p_1}} \cdot \frac{\text{erfc}^{-1}(2p_1)}{\sqrt{\eta^{(el)}_\infty}} \quad \text{for} \quad R_c \to 0 . \quad (17)$$

As expected, at very low values of $R_c$ a factor 10 reduction of $p_1$ corresponds to a 5 dB increase of $G$. Furthermore, a gain is only available if $p_1$ is steadily reduced with $R_c$. Empirically one would argue that, having already very low $p_1$ values, a further reduction of $p_1$ requires the same reduction of $R_c$. However, as indicated in the left diagram of Fig. 3, $H(X)$ and $R_c$ exhibit the same slope over $p_1$. Since $H(X) \approx -p_1 \log_2(p_1)$ for $p_1 \to 0$, it follows that

$$G \cdot \sqrt{R_c} \sim \sqrt{-\log_2(p_1)} \quad \text{for} \quad R_c \to 0 . \quad (18)$$

In other words: even at very low coding rates, the gain over $R_c$ is slightly larger than 5 dB per decade, but most of the gain available is simply due to the "shortened" pulses.
5. CODING GAIN FOR PULSE-POSITION MODULATION

PPM is a very popular modulation scheme for wireless optical transmission. First of all, orthogonal PPM provides a power gain compared to the OOK-reference — even without additional coding. Furthermore, for small numbers \( M \) of PPM-symbols used, the transmitted signal contains much less low frequency spectral components than uncoded OOK, which is preferable for wireless optical transmission [6].

5.1. Transmission model for PPM

To discuss the coding gain limits for \( M \)-PPM, the proposed OOK-model has to be extended first. The transmitted signal is now

\[
p_{tx}(t) = \sum_{i} S \phi_i(t - iT_{PPM}).
\]

(19)

Depending on the \( i \)-th \( M \)-level symbol \( s_i \in \{0, 1, \ldots, M - 1\} \), one out of \( M \) orthonormal signals \( \phi_j(t - iT_{PPM}) \) is chosen and transmitted. Orthogonality is achieved by placing the pulse \( \psi(t) \) defined in (2) at one of \( M \) distinct positions \( jT \)

\[
\phi_j(t) = \psi(t - jT), \quad j = 0, 1, \ldots, M - 1.
\]

(20)

The PPM-symbol duration \( T_{PPM} \) and the original binary symbol interval \( T \) are related as follows:

\[
T_{PPM} = M \cdot T,
\]

(21)

where \( T \) is usually denoted as chip interval in the case of PPM. With \( p_1 = 1/M \), the average optical power is already defined in (3). The receiver consists of \( M \) different filters \( \psi_j(t) \) whose outputs are sampled at \( t = iT_{PPM} \) and used to estimate the transmitted signal. If the \( M \) sampled filter-outputs are treated as vectors, the received discrete-time signal vector \( Y \) is given as

\[
Y = X + N,
\]

(22)

where \( X = \{x_0, x_1, \ldots, x_{M-1}\} \) is the signal component and \( N \) is the noise component. With \( X \) defined in (11), the signal vectors are given as follows:

\[
x_0 = [\hat{X} \ 0 \ 0 \ \ldots \ 0]^T, \quad \ldots, \quad x_{M-1} = [0 \ 0 \ \ldots \ 0 \ \hat{X}]^T.
\]

(23)

The noise vector \( N \) has \( M \) i.i.d. noise components statistically described in (5).

5.2. Uncoded PPM

We still treat \( R_c = T/T_h \) as the coding rate. Consequently, even if no additional coding is applied to the PPM-symbols, the code rate is

\[
R_c = \log_2(M)/M.
\]

(24)

This makes sense, because PPM can be also considered as a linear code combined with OOK, where each of the \( M \) code words consists of \( M \) binary symbols. Using this definition of \( R_c \), we can interpret \( 1/R_c \) as a direct measure of the required bandwidth. Taking \( \phi_j(t) \), \( j \in \{0, 1, \ldots, M - 1\} \), as a set of \( M \) orthonormal base functions, the Euclidian distance between signal vectors \( x_i \) is

\[
d_{Eucl} = \sqrt{X} \cdot \hat{X} = X_{ref} \cdot \sqrt{\frac{M \log_2(M)}{2} \cdot \frac{1}{G}}.
\]

(25)

for the uncoded case. This yields an upper bound of

\[
p_c \leq \frac{M}{2} \cdot \left( \frac{M}{2(M - 1)} \right) \cdot \text{erfc} \left( \frac{d_{Eucl}}{2\sqrt{N_0}} \right),
\]

(26)

where the term in the brackets comprises the symbol error to bit error ratio. Therefore, PPM without additional "outer" coding achieves a gain of

\[
G \geq \text{erfc}^{-1}(2p_c) \sqrt{\frac{M \log_2(M)}{2}} \approx \sqrt{\frac{M \log_2(M)}{2}}.
\]

(27)

5.3. Coded PPM

With \( R_c = T/T_h \), the requirement for the mutual information \( H(X; Y) \) per PPM-symbol is now

\[
H(X; Y) = H(Y) - H(Y|X) = R_c \cdot M.
\]

(28)

Since the conditional probability

\[
I_{Y|X}(y|x_i) = \left( \frac{1}{\pi N_0} \right)^{M/2} \exp \left( -\frac{(y_i - \hat{X})^2}{N_0} \right).
\]

\[
\prod_{j=1}^{M} \exp \left( -\frac{y^2}{N_0} \right), \quad \forall i \in \{0, 1, \ldots, M - 1\}
\]

(29)

equal to the joint probability of the corresponding noise vector \( n = y - x_i \), the irrelevance (supposing PPM symbols with equal probability) is now

\[
H(Y|X) = H(Y|x_i) = 0.5 \cdot M \cdot \log_2(\pi e N_0) \quad \forall i.
\]

(30)

Similarly, the entropy \( H(Y) \) at the output is

\[
H(Y) = -\int_y f_Y(y) \log_2 f_Y(y) dy = \log_2(M) - \int_y f_Y(X(y|x_i)) \log_2 \sum_{j=1}^{M} f_Y(X(y|x_j)) dy.
\]

(31)

Since it is impossible (at least impractical) to solve the \( M \)-dimensional integral in (31), we used Monte-Carlo simulations to obtain \( H(Y) \) as suggested in [8]. We first generated a large number \((10^6)\) of random vectors \( y \) according to the conditional probability function \( p(y|x_1) \). Then the logarithm in (31) was calculated for all the \( y \)-vectors and averaged over the total number of random vectors.

5.4. Results

Fig. 6 shows the coding gains attainable with \( M \)-PPM. It should be noted that, as a result of our definitions, a value \( R_c = \log_2(M)/M \) corresponds to uncoded PPM-transmission. The associated gains derived in (27) can be easily acquired by means of the origins of the curves marked with a “x”. Uncoded 4-PPM achieves a 3 dB gain compared to our OOK-reference, 16-PPM a 7.3 dB gain. These values lie approximately 6 and 4.5 dB, respectively, below the theoretical limit for binary transmission (dashed line).

If PPM is combined with an additional "outer" code, the gains clearly converge for \( R_c \rightarrow 0 \) to fixed values, since the probability of the logical "1" pulses \( p_1 \) remains fixed for each \( M \)-value.
binary transmission, under the assumptions of a fixed average optical power and additive white Gaussian noise. We first developed the ideal case, the code rate of the additional outer code could be quite small.

At distinct code rates close to the maximum value attainable for ideal binary transmission if the OOK-DC component, being 3 dB below the overall waveform (representing logical ones), whose integral effectively measures the influence of the pulse shape on the required power. For a fixed symbol rate it was shown, that the required power can be reduced by a factor $\sqrt{a}$ if the pulse width is reduced by a factor $a$.

The maximum coding gains for optimized OOK transmission where derived. A coding rate of 1/2 promises theoretically a gain of 9.2 dB, a code rate of 1/10 a gain of 15 dB. In contrast to linear channels, the code gain grows unbounded. However, at code rates smaller than 1/10, the gain is dominated by the "shaping gain", which is always available if the code rate and with it the pulse density are reduced. If, for example, the code rate is reduced from 1/10 to 1/1000, the additional gain attainable with optimized OOK is about 17.5 dB, which is only 2.5 dB more than the nominal "shaping gain" of 15 dB.

In the final section orthogonal PPM was introduced, which ensures specific spectral characteristics. It was shown, that at specific code rates the gains available with coded PPM come close to the limits for binary transmission — supposing a relatively large number of PPM-symbols.

6. CONCLUSIONS

In the article we derive the maximum coding gain attainable with binary transmission, under the assumptions of a fixed average optical power and additive white Gaussian noise. We first developed an OOK transmission model and discussed the uncoded OOK reference scheme. Useful insights in the special characteristics of the considered quadratic type of channel where obtained. We have shown that the required optical power does not increase linearly with the bit rate, but in fact with its square root. Furthermore, in the opposite to linear channels, the required power depends also on the pulse shape. We have introduced a normalized version of the waveform (representing logical ones), whose integral effectively measures the influence of the pulse shape on the required power. For a fixed symbol rate it was shown, that the required power can be reduced by a factor $\sqrt{a}$ if the pulse width is reduced by a factor $a$.

The maximum coding gains for optimized OOK transmission are derived. A coding rate of 1/2 promises theoretically a gain of 9.2 dB, a code rate of 1/10 a gain of 15 dB. In contrast to linear channels, the code gain grows unbounded. However, at code rates smaller than 1/10, the gain is dominated by the "shaping gain", which is always available if the code rate and with it the pulse density are reduced. If, for example, the code rate is reduced from 1/10 to 1/1000, the additional gain attainable with optimized OOK is about 17.5 dB, which is only 2.5 dB more than the nominal "shaping gain" of 15 dB.

In the final section orthogonal PPM was introduced, which ensures specific spectral characteristics. It was shown, that at specific code rates the gains available with coded PPM come close to the limits for binary transmission — supposing a relatively large number of PPM-symbols.

7. REFERENCES


